

## GRAPH THEORY: CLASS 1

- 1) Find an Euler trail in the graph  $G$ .
  
- 2) Show that  $K_{2,3}$  and  $K_4$  are planar. What do you think about  $K_5$ ?
- 3) Show  $1 + 3 + 5 + \dots + (2k - 1) = k^2$ .
- 4) Prove that if the numbers  $1, 2, \dots, 12$  are randomly positioned around a circle, then some set of three consecutively positioned numbers must have a sum of at least 19.
- 5) Show if  $n$  is odd then  $n^2 + 1$  is even.
  - a) By using direct proof.
  - b) By using contrapositive.