

## NUMBER THEORY: CLASS 23

### 1. EXERCISE

1) Show explicitly the bijection match using conjugation of  $p(n|m \text{ parts}) = p(n| \text{ greatest part is } m)$  for  $n = 8$  and  $m = 4$ .

2) Prove  $p(n| \leq m \text{ parts}) = p(n| \text{ all parts } \leq m)$ .

The following two problems are refinement of Euler's Theorem.

3) Let  $N = \{1\}$ . Find the set  $M$  such that

$$p(n| \text{ parts in } N) = p(n| \text{ distinct parts in } M) \text{ for all } n \geq 1 .$$

4) Let  $N = \{1, 3\}$ . Find the set  $M$  such that

$$p(n| \text{ parts in } N) = p(n| \text{ distinct parts in } M) \text{ for all } n \geq 1 .$$

5) A partition function  $p(n)$  also have a nice relation between their values and congruence.

Use command in the Maple program to conjecture the relation between the values of  $p(5n + 4)$ ,  $p(7n + 5)$  and  $p(11n + 6)$  and theirs congruence.

Try:

```
> with(combinat);
```

```
> seq(numbpart(5 * n + 4), n = 1..10);
```